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Study of Phase Transitions
in Perovskite-Type Crystals

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STUDY OF PHASE TRANSITIONS IN PEROVSKITE-TYPE CRYSTALS

The discovery of the ferroelectric activity of BaTiO₃⁽¹⁾ has attracted many researchers to further studies of related percvskite-type crystals with molecular formula ABO₃. The perovskite-type crystals which have shown ferroelectric activity can be divided into at least three classes: one is $A^{+2}B^{+4}O_{3}$, such as BaTiO₃; the second is $A^{+1}B^{+5}O_{3}$, such as KNbO₃; and the third is $A^{+1}A^{+3}B_{2}^{+4}O_{6}$, such as KLa(TiO₃)₂. Other perovskite-type materials have also been examined elsewhere, but their characteristics are not considered here because we have had no experience with them.

In the first group we have been studying the properties of PbHfO₃, and have found that this crystal is an antiferroelectric of the same type as PbZrO₃. In the second group we have been interested in the NaNbO₃-KNbO₃ system, which shows very occuliar properties, and is discussed in some detail below.

A. PHASE TRANSITIONS IN POHFO3

I. INTRODUCTION.

Recent studies of PbTiO₃(2) and PbTrO₃(3) have revealed interesting dielectric properties and relations of these to the crystal structures of these perovskite-like compounds. PbTiO₃ is a ferroelectric with a Curie point of 490°C, and this is very similar to the much-studied Curie point of BaTiO₃ at 120°C. The crystal structure (4) of PbTiO₃ is distorted to a tetragonal lattice below its Curie point, and with c/a=1.06 at room temperature; it is of course cubic above its Curie point. The dielectric properties of PbZrO₃, on the other hand, have shown that this crystal is not ferroelectric but rather antiferroelectric with a Curie point at 230°C, notwithstanding the close resemblance of the permittivity vs. temperature curve of this crystal to those of BaTiO₃ and PbTiO₃. The crystal structure (4) of PbZrO₃ is distorted to a tetragonal cell, but the axial ratio c/a is less than unity (0.99) -- in contrast with BaTiO₃ and PbTiO₃ in which c/a is bigger than unity.

No satisfactory explanation has been given of the reason why such an essential difference in dielectric and structural properties can be observed in these very closely related perovskite crystals. Although there is no doubt that the large polarizability of the Pb ion in both compounds contributes to these peculiar phenomena, the essential difference in these compounds is the differences in ionic radii and polarizabilities of B ions in the ABO3 crystals which have Pb as the common A ion. This fact suggests that the further study of lead compounds with different B ions, such as PbHfO3 and PbThO3, may give more information about this interesting phenomenon. The Hf ion has a rather close ionic radius to Zr and, at the same time, a

different (probably larger) polarizability. Up to now, however, few studies were carried out on hafnium compounds because of difficulty of obtaining pure hafnium. We have carried out a dielectric and structural study of PbHfO3, and observe that this crystal shows antiferroelectric behavior of the same type as PbZrO3.

II. SPECIMEN PREPARATION.

Ceramic PbHfO₃ was prepared from PbCO₃ and HfO₂. Equimolar proportions of these ingredients were mixed well and fired at about 1200°C after preliminary firing at about 1000°C. The specimen was pressed into a pellet with a pressure of about 10⁸ gm/cm². The fired specimen is a hard ceramic with a yellowish color.

The first difficulty in obtaining good PbHfO3 arises from the difficulty of obtaining pure HfO2. One gram of HfO2 was supplied by Fairmount Chemical Co., which company claimed a purity of 99.5% HfO2, with 0.3% ZrO2 and 0.2% TiO2. Rough estimation by spectrographic examination, carried out by Dr. R. Hayes of the Pennsylvania State College, indicating the existence of Zr in an amount from 0.03% to 0.3%. A second and rather unexpected difficulty is the very severe evaporation of PbO from the specimen during the course of firing. A similar difficulty was encountered in the case of PbTiO3, and also (more pronounced) in the case of PbZrO3. But in PbHfO3 the evaporation is so severe that the color of the surface of the sintered specimen changes to white and the powder photograph of the surface material shows some weak diffraction lines due to HfO2. Though the small supply of HfO2 did not allow us to develop a satisfactory method for preventing the evaporation, the following procedure was helpful in obtaining a rather good specimen. A

few percent of PbO was added in excess of equimolar proportion, and firing was carried out rather quickly in a Pt crucible with a cover to retard the evaporathe tion of PbO. The white surface of specimen was removed by polishing, and the uniform yellow interior part was used for the dielectric and structural studies. No chemical analysis was carried out of the final specimen, and this should ultimately be done.

III. CRYSTAL STRUCTURE AT ROOM TEMPERATURE.

Powder photographs of PbHfO₃ were taken with a Norelco powder camera (11.4 cm. diameter), using Cu Ka radiation. Diffraction lines clearly show a distorted perovskite structure, and all multiplets can be well explained by assuming a tetragonal cell with c/a<1. The lattice constant and axial ratio calculated from (510), (431) and (422) lines are shown below, together with data for PbTiO₃ and PbZrO₃.

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Crystal	a-axis	c/a	unit cell volume
PbTiO ₃	3•905	1.063	63•30
PbZrO3	4.159	0.988	71.06
PbHfO3	4.136	0.991	70.06

 $(\lambda=1.5405\text{Å})$ was used as the Cu Ka₁ wave length. The values for PbZrO₃ and PbTiO₃ were recalculated from Megaw's (4) data with this wave length.)

It is to be noted here that the c/a ratio for PbHf03 is less than unity, as in PbZrO3. Moreover, some extra lines can be observed in the PbHfO3 powder photograph besides the main lines due to a perovskite structure. Careful

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came character of superstructure line not only in spacing but also is relative intensities. These facts strongly suggest that Pblifo, has the same type of superstructure as Pblro, which latter was attidied by sawaguchi et al (5) using a single crystal method. These investigators found an antiparallel displacement of 2r (or Pb) ions as shown in Fig. 1. Thus we can expect antiferrom electricity in PbHro, similar to that in Pb2ro, Rough estimation of the intensities of diffraction patterns of these two crystals are shown in Fig. 2. Superstructure lines are indicated by open circles.

Basides these very close resemblances between one A-ray powder patterns of these two compounds, we can find a large difference in the ratio of the intensity of odd $N = h^2 + K^2 + 1^2$ to that of even N, as easily seen is Fig. 2. This can be explained well by the difference in the stemic scattering factors of Zr and Hf. Another interesting result is that the unit cell volume of PbHfO, is smaller than PbZrO, which obviously shows that the Hf 4+ ion is slightly smaller than Zr 4+ ion.

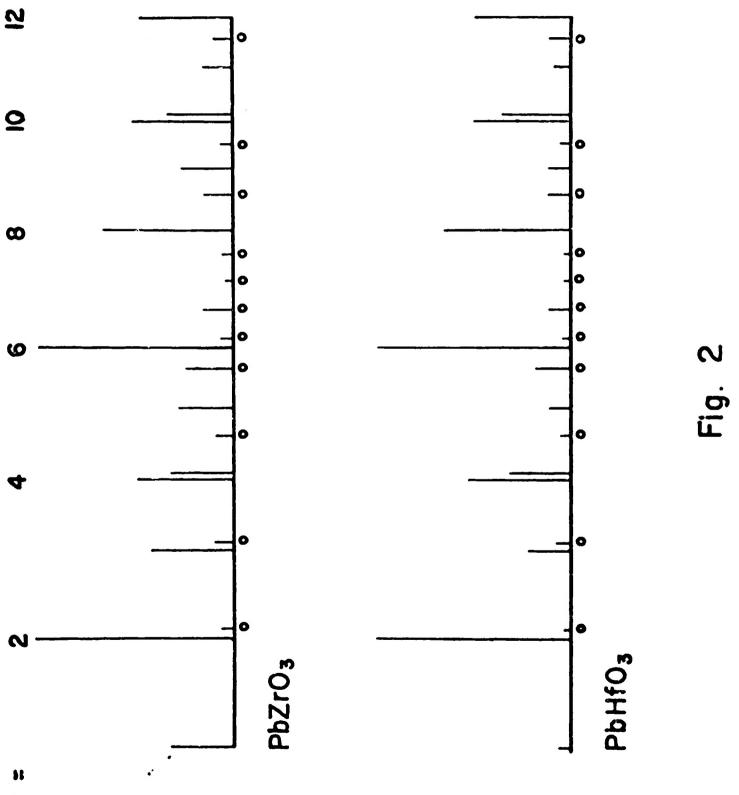
IV. DIELECTRIC PROPERTIES.

The specimen for dielectric measurement was a disk 1 mm. in thickresponding am. 2 in area, and aliver pasts was applied to both surfaces as electrodes. Fig. 3 shows the dielectric constant vs. temperature curve at a frequency of 10-kc/sec.

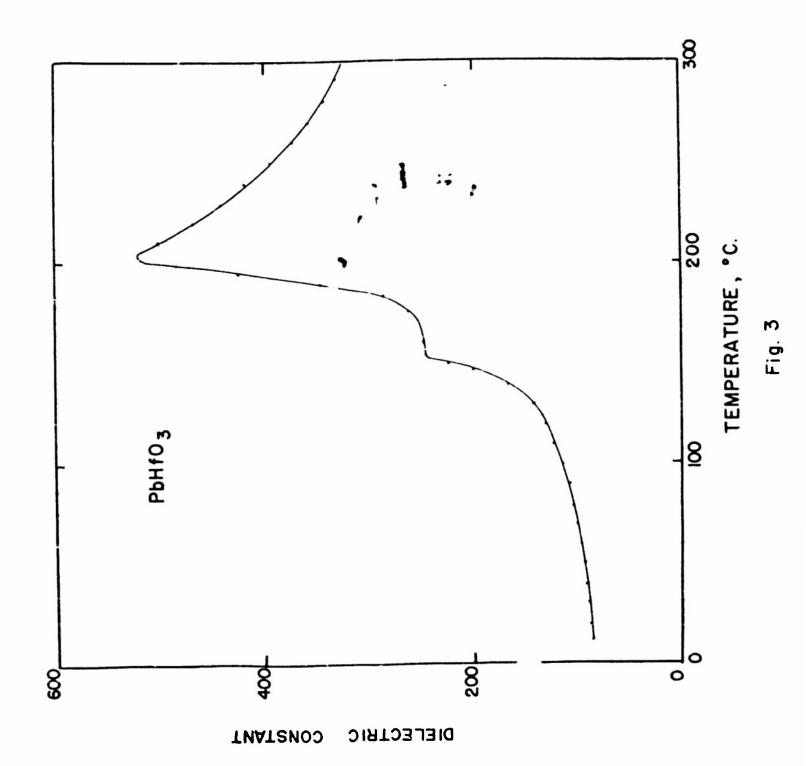
This curve shows two anomalies in the temperature dependence of dielectric constant: one is a small anomaly at 160°C, which suggests the existence of some kind of phase change; another is a pronounced peak at 210°C, above which the crystal becomes paraelectric. From the crystal structure we

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L O	5	9	07	لک	^
<i>وع</i> ا	2	2	Q.I	Q.	4.15×4Å-
3	0]	2	K _O	2	-4.15
50	Q ⁷	0غ	K 0	K	
2	1 50	O₁	21	K 0	2

plane. Although the true symmetry may be orthorhombic, we choose here tetragonal axes. An arrow shows the displacement of a heavy ion (probably a Pb ion). Fig. 1 A model of the atomic arrangement of PbZrO₃, (001)



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is no doubt above the paraelectricity at my 210°C. To study the dielectricity at my 210°C. To study the dielectric response of the intermediate phase we as mined the replantation was electric field relation under an a.c. amplitude at 10 km/cm. As shown in Fig. 1.

The P-E relation is almost linear in all three proofs except for a slight upward curvature just below the Curie point. No introduction hysteresis loops were observed even just below the Curie point.

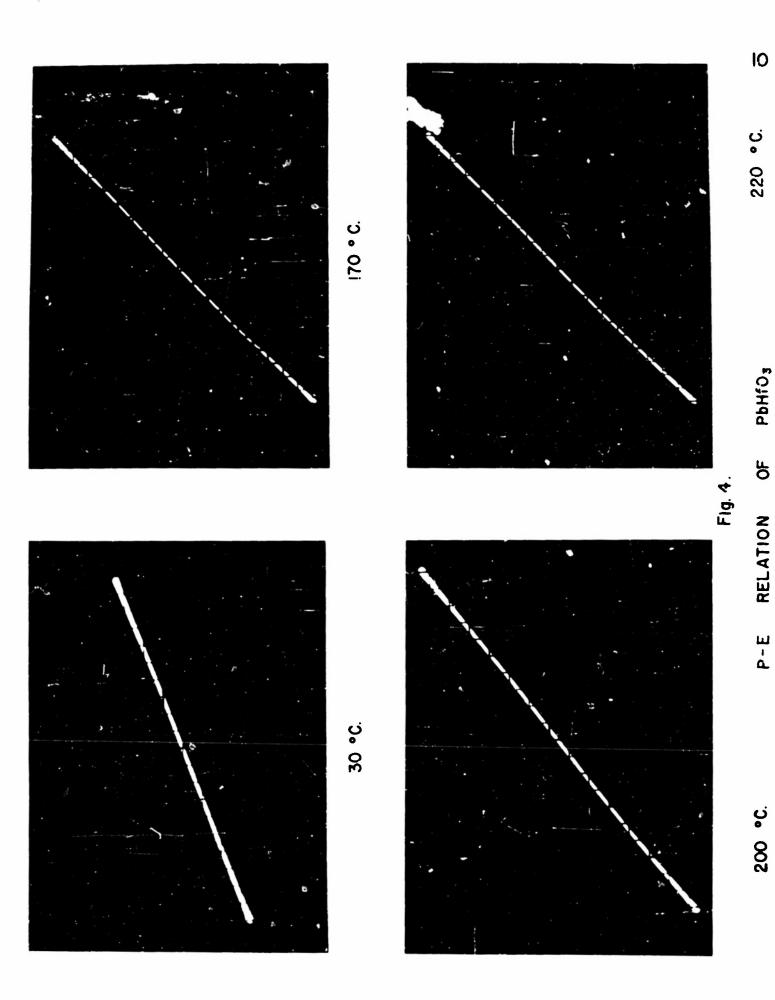
at room temperature, that the lowest phase below intermediate phase is another antiferroelectric phase (AII) which must diar from phase AI in some

Above the Curie point the temperature depend to a of the dielectric constant obeys the Curie-Weiss law $E = 1/(0-T_0)$, with $C = 1.0 \times 10^5$, $T_0 = 110^{\circ}C$; this Curie constant is very close to those of Ballio and $C = 1.0 \times 10^5$.

V. STRUCTURAL CHANGES AROUND THE PHASE TRANSITION .

As shown in Fig. 3, the dielectric const : was temper ature curve shows two anomalies, indicating two phase changes. Now, the later asting problem is the crystal structure of PbHfO₃ in the intermediate phase became these two phase changes at 160°C and 210°C. To check this pint, a series of powder photographs at various temperatures were taken by using the Unicam (19 cm.) high-temperature X-ray powder camera.

Below 160°C the diffraction patterns are essentially the same as the room temperature, except that the c/a ratio tends toward unity and, at the same time, the intensity of extra lines decrease: gradually as 160°C is

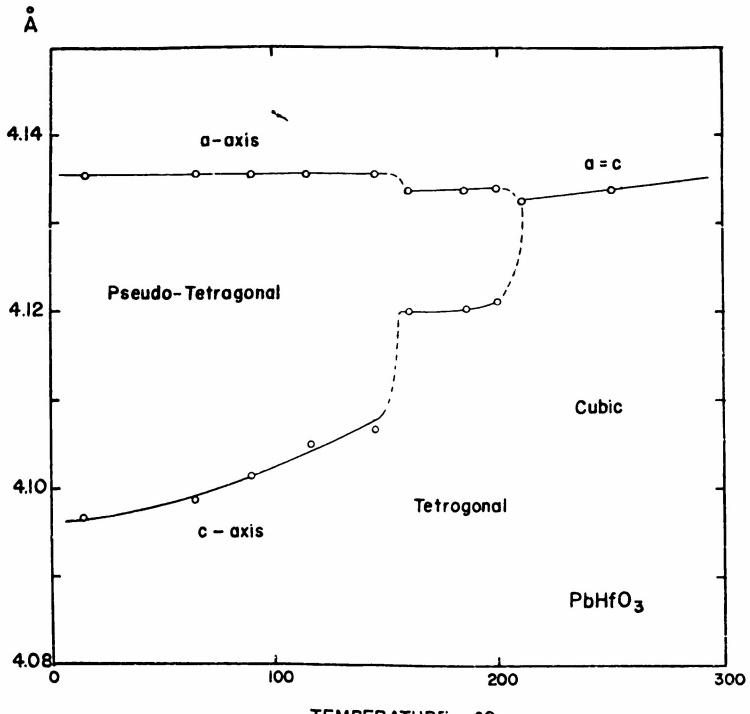


approached from below. Above 210°C the photographs show a cubic perovskite lattice without any superstructure lines.

The diffraction patterns at the temperature region in the intermediate phase is very close to a cubic pattern, and we can observe multiplets only in a few high-angle lines. In such a case it is rather difficult to determine the structure by using powder photographs only, and we tried to explain these multiplets only in a few high-angle lines, by assuming simple possible cases such as tetragonal c/a < 1, orthorhombic and rhombohedral. We found that the multiplets can be well explained if we assume a tetragonal lattice with c/a < 1. The lattice parameters and c/a calculated from (510), (431) and (422) lines are shown in Fig. 5 and Fig. 6.

The dielectric test showed that the dielectric properties of this middle phase may be antiferroelectric. Careful examination of powder photographs reveals a few rather weak but definite superstructure lines, which are different from those found at room temperature both in spacing and in relative intensity.

The above results show that the change at 160°C is a phase transformation from tetragonal to another tetragonal phase, with a discontinuity in the axial ratio c/a. This seems rather strange. However, we must notice here that the powder pattern at room temperature indicates a tetragonal lattice with c/a < 1; but the structural study of a single crystal of PbZrO₃ showed, as seen in Fig. 1, that the true symmetry of the crystal is not tetragonal but orthorhombic. We can conclude that the phase transition at 160°C is a phase change from orthorhombic phase to a tetragonal phase, caused by some rearrange-

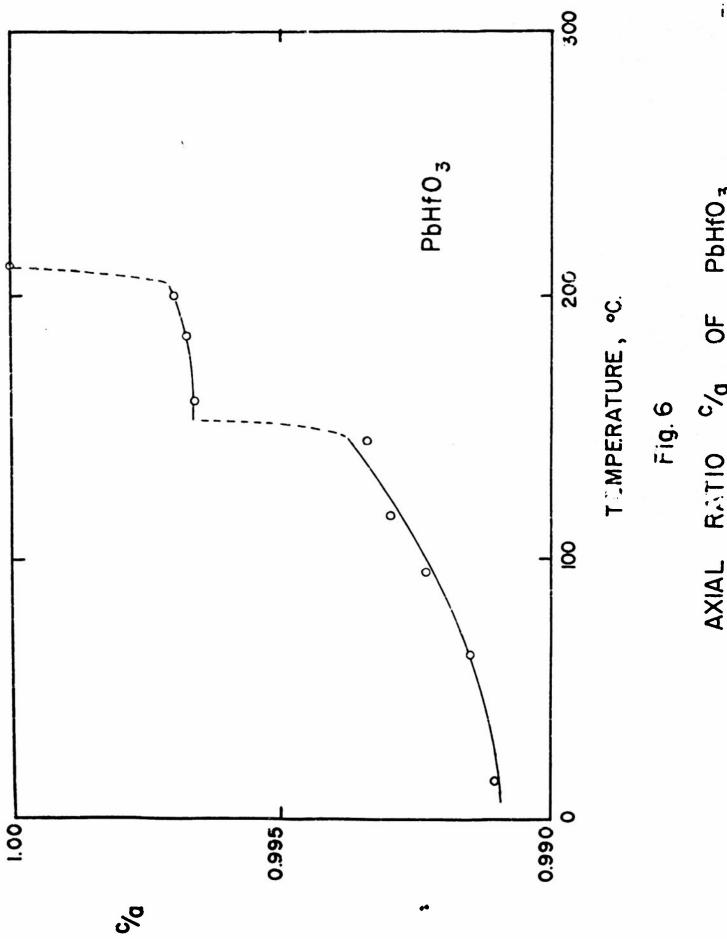


TEMPERATURE, °C.

Fig. 5

LATTICE PARAMETERS OF POHTO3

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ment of the antiparallel displacement of iong. The detailed study of the crystal structure of the intermediate phase must await angle crystal study.

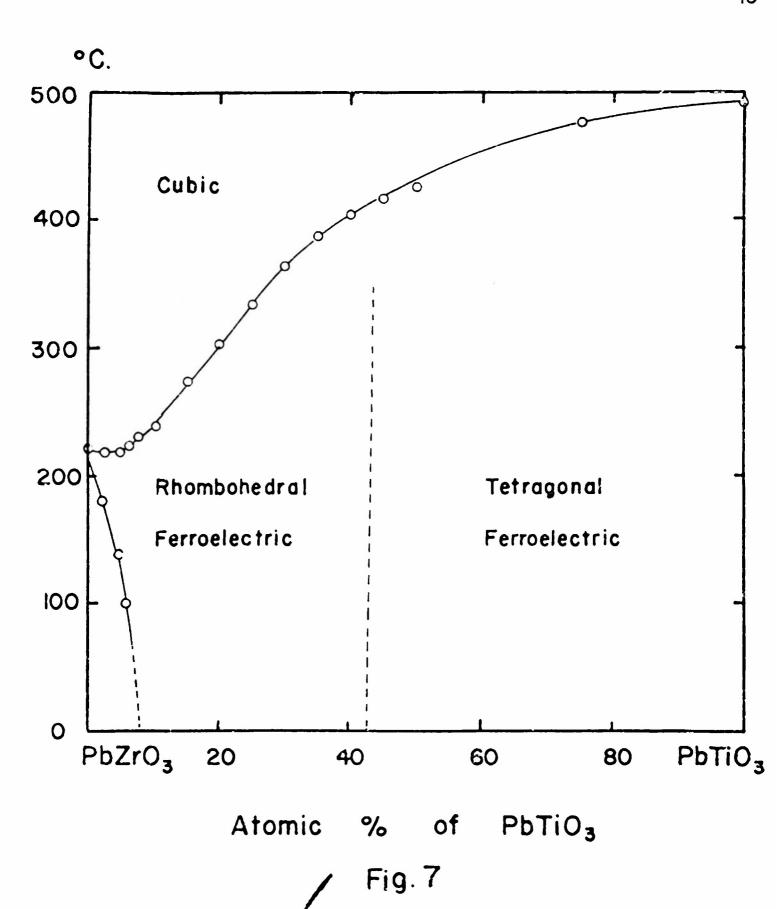
Summarizing, the phase changes in PbHfO3 are shown in schematical form as follows:

Antiferroelectric I	Antiferroelectric II	Paralectric
1.60°C	210°0)
Orthorhombic (pseudo-tetragonal)	Tetragonal	Cubic

VI. DISCUSSION.

The foregoing experimental results has shown that PbHfO₃ is antiferroelectric with a Curie point of 210°C. The interesting and rather unexpected results of these observations are: firstly, the Curie point of
PbHfO₃ is very close to that of PbZrO₃, notwithstanding the difference in the
ionic radii and polarizabilities of these crystals; and, secondly, the existence of the antiferroelectric intermediate phase between the lowest and
paralectric phases. At present it is difficult to explain these frots; but
the following consideration may be helpful.

The recent studies of PbZrO₃⁽³⁾ and solid solutions⁽⁶⁾ derived from PbZrO₃ by replacing Pb or Zr ions by other suitable ions show the rather peculiar phase diagrams as shown in Figs. 7 and 8. In the cases of Pb(Zr-Ti)O₃ and (Pb-Ba)ZrO₃, the rhombohedral ferroelectric intermediate phase was observed, and, on the other hand, in the case of (Pb-Sr)ZrO₃, the tetragonal antiferroelectric intermediate phase was found. A comparison of superstructure lines in the intermediate phases of (Pb-Sr)ZrO₃ and PbHfO₃ showed that the both compounds have essentially the same superstructure; consequently they are probably the same phase.



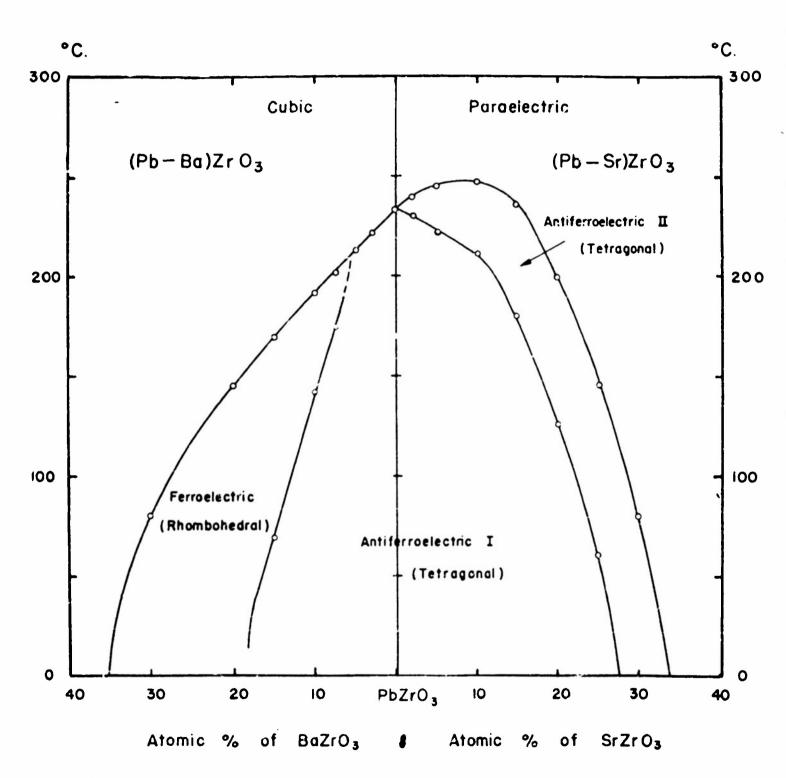


Fig. 8

Proper explanations of these many experimental results are not yet possible. However, if we assume that the small ionic radius and large polarizability of Hf ion compared with those of PbZrO₃ have almost compensated each other, we can possibly explain -- or at least expect -- the small change of the Curie point from PbZrO₃ to PbHfO₃, and the existence of the intermediate phase in PbHfO₃.

B. STUDY OF NaNbo3-KNbo3 SYSTEM

I. INTRODUCTION.

The Terroelectric phase transitions in perovskite niobates were studied by Matthias and Remeika (7) and by Wood (8), with the following results:

KnbO3: orthorhombic 220°C tetragonal 430°C cubic.

NaNbO3: orthorhombic 370°C tetragonal 480°C cubic.

Concerning KNbO3, a recent study (9) in our laboratory has revealed the existence of a phase change at -20°C, showing the existence of a lower rhombohedral phase which gives this crystal the complete similarity to the phase changes in BaTiC3.

On the other hand, the situation with NaNbO₃ is rather confusing. First, structural study of this crystal at room temperature by Vousden⁽¹⁰⁾ showed the non-polar structure which rejects, in any case, the existence of ferroelectricity in this crystal. Second, the optical and X-ray studies by Wood has suggested another higher phase change around 640°C, in addition to two phase transitions at 370°C and 480°C; and an optical study by Vousden led that investigator to report two phase changes at 300°C and 600°C.

These two questions: whether NaNbO3 is really ferroelectric or not, and what transitions really exist in NaNbO3 at high temperatures, suggested

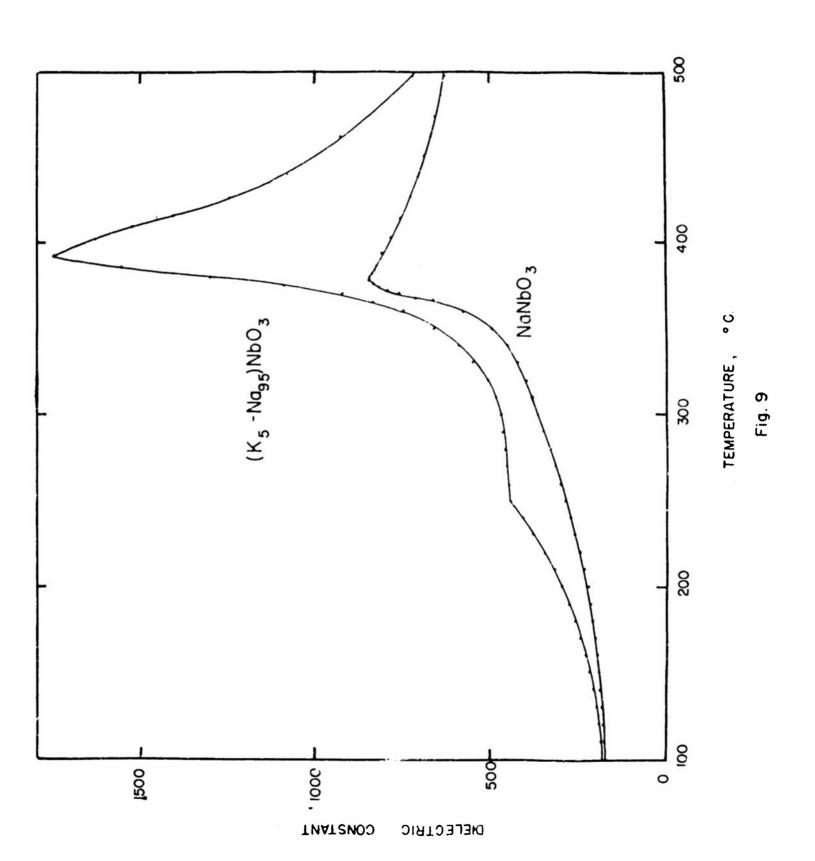
the need for a further study of NaNbO3 and its aclid solutions with KNbO3.

II. DIELECTRIC PROPERTIES.

The specimen used for the following experiments were prepared from K_2CC_3 , Na_2CO_3 and Nb_2O_5 . These ingredients were mixed in desired proportions and fired at various temperature, which varied from $120C^C$ C for pure $NaNtO_3$ to 1000^O C for pure $KNbO_3$ after preliminary calcination. It is rather difficult to obtain hard ceramics, especially toward the pure $KNbO_3$ side; but applying a large pressure to the pellet and adjusting the firing temperature to just below the melting point, we could obtain good ceramics which are hard enough for dielectric tests. Silver paste was applied to both surfaces as electrodes.

Dielectric constant vs. temperature curves were measured at 10 kc/sec and 10 v/cm. Some of the results are shown in Fig. 9 to 11. In NaNbO3 we observed only one anomaly at 370° C, in contrast with the two phase changes at 370° C and 480° C previously reported by Matthias and Remeika. When we replace small amount of Na in NaNbO3 by K, we observe two anomalies as shown in Fig. 9 for $(K_5-Na_{95})NbO_3$. With increasing K concentration, these two anomalies were observed always around 200° C and 400° C. The dielectric constant of pure $KNbO_3$ shows two anomalies at 320° C and 430° C, in good agreement with the previous data of Matthias and Remeika.

From these measurements, the phase diagram of (K-Na)NbO₃ was obtained as shown in Fig. 12. To study the ferroelectricity of each phase shown in this diagram, we examined the hysteresis loops of a number of solid solutions, and some of the results are shown in Fig. 13. Above the highest phase line, as expected, the P-E relation is always linear. In the intermediate phase we can get good hysteresis loop even in the specimen near the pure NaNbO₃ side.





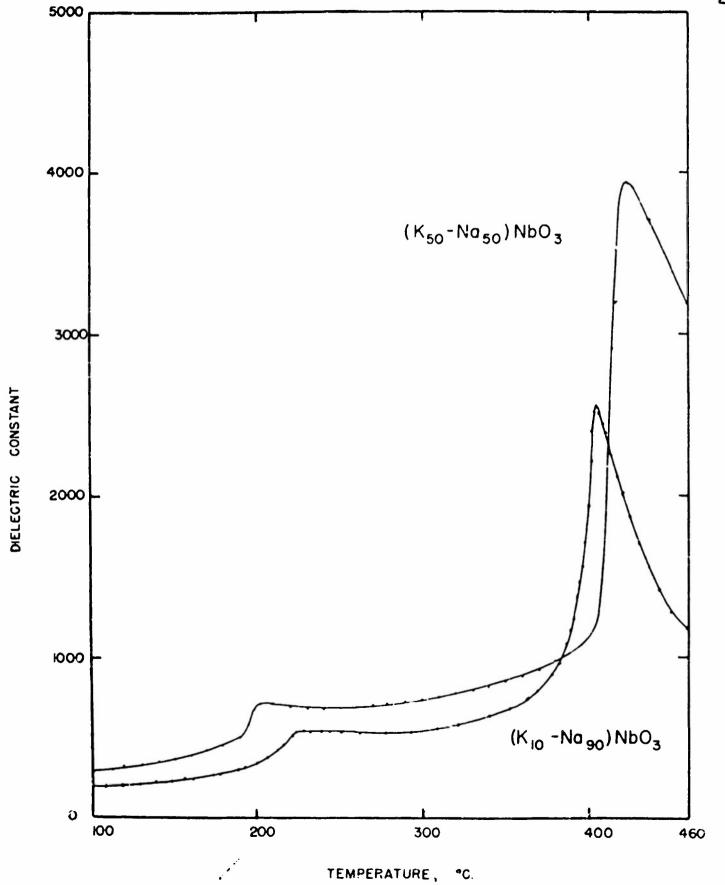


Fig. 10

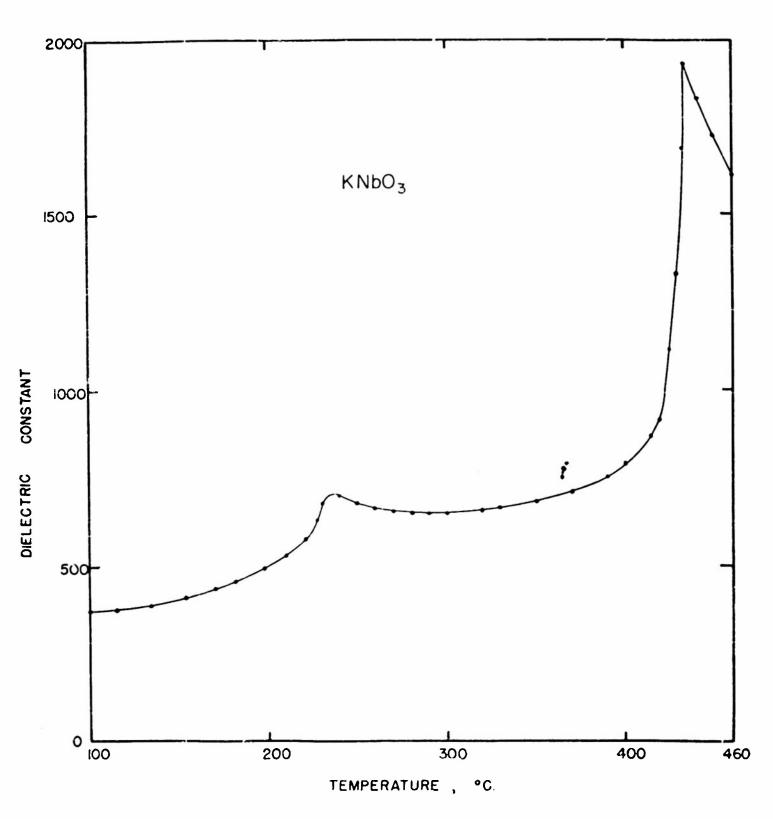
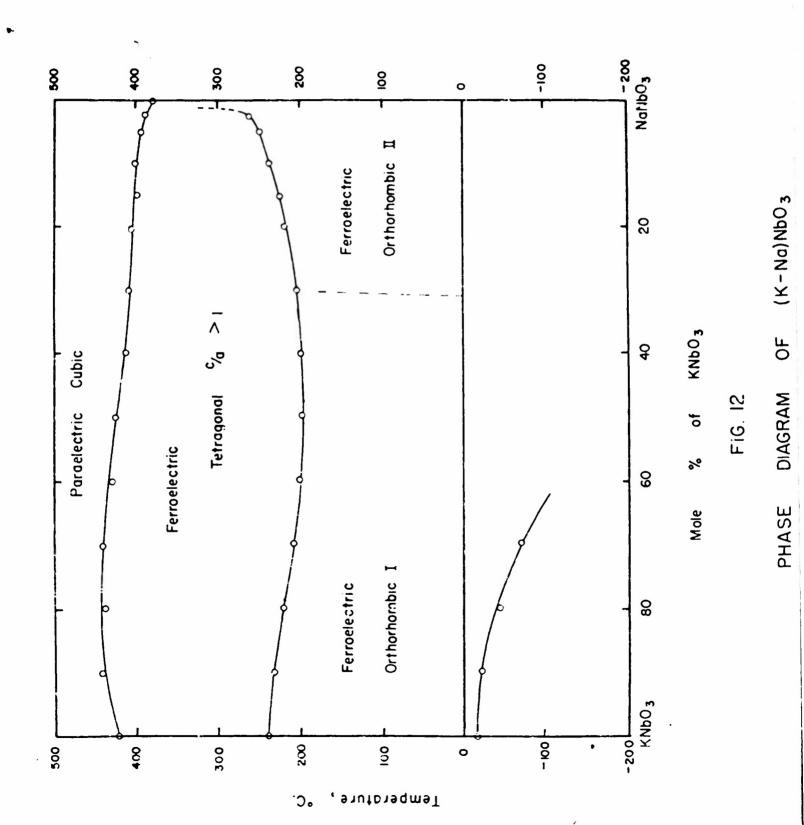
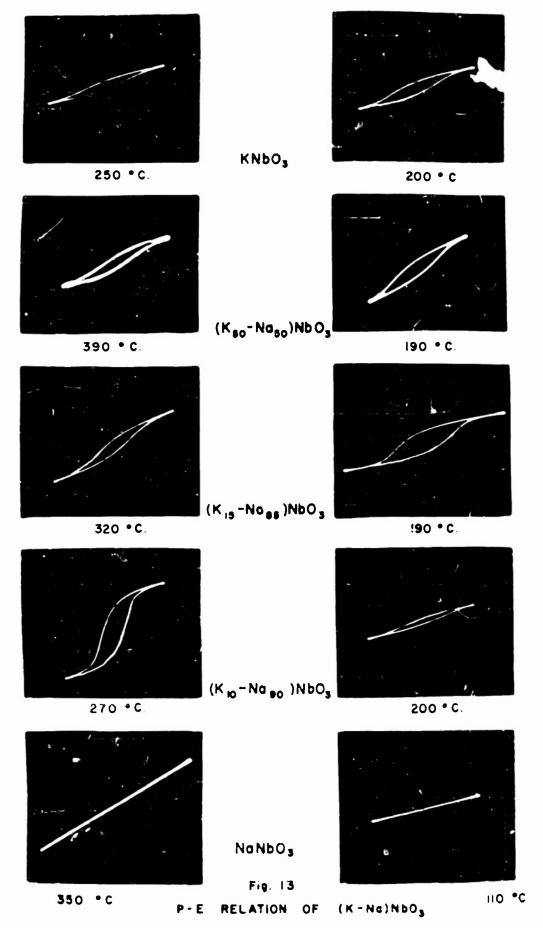


Fig. 11





In the lowest phase, we can get ferroelectric hysteresis loops, except for a region very close to pure NaNbO3; but, comparing the loops of the same specimen at the intermediate phase, the operative force is larger and the spontaneous polarization is smaller. As shown in Fig. 13, the hysteresis loop at the lowest phase becomes more and more ambiguous as we approach pure NaNbO3, although the solid solution such as (K10-NaO0)NbO3 and (K5-NaO5)NbO3 show good loops in the intermediate phase. No hysteresis loops were observed in pure NaNbO3. From these results we can conclude the paraelectric character of the highest phase, ferroelectricity in the middle phase, and also ferroelectricity in the lowest phase except for pure NaNbO3.

III. STRUCTURAL STUDY.

Before discussion of this phase diagram of the (Na-K)NbO₃ system, we must examine the important point whether this (K-Na)NbO₃ system is really forming a solid solution, because the difference of ionic radii of K and Na is large enough to give us this doubt.

(A) Crystal Structures at Room Temperature.

The crystal structures of KNbO₃ and NaNbO₃ at room temperature were studies by Wood⁽⁸⁾ and by Vousden⁽¹¹⁾. Both crystals show the same type of orthorhombic distortion from cubic perovskite, but NaNbO₃ differs from KNbO₃ in one important point, namely, the patterns show "extra lines" which requires the assumption of some kind of superstructure. This superstructure was studied by Vousden⁽¹⁰⁾, who reported the non-polar structure of this crystal, and drew some strange conclusions from this.

A series of powder photographs were taken with the various compositions covering the whole range of the (K-Na)NbO3 system. It is rather difficult

to get clearly resolved photographs especially on the NaNbO3 side. This is presumably due to the large difference of ionic radii of K and Na. which inevitably causes a large internal strain. Especially on the NaNbO3 side the replacement of the small Na ion with the large K ion may cause more strain than in the opposite case near KNbO3.

From the comparison of the photographs of whole solid solution range, we can reach following conclusions:

- (1) The lattice constant decreases gradually from KNbO3 to NaNbO3, and no evidence was observed for the existence of a mixed phase.
- (2) Powder photographs of solid solutions ranging from $KNbO_3$ to $(K_{\bullet 50}-Ne_{\bullet 50})NbO_3$ show sharp lines, and essentially the same characteristics as pure $KNbO_3$.
- (3) From pure NaNbO3 to $(K_{\bullet 15}^{-Ng}_{\bullet 85})$ NbO3, the diffraction patterns are essentially the same as pure NaNbO3; i.e., they show the same type of extra lines.
- (4) In the intermediate region between $(K_{-40}-Na_{-60})Nb0_3$ to $(K_{-80}-Na_{-20})Nb0_3$ the diffraction lines are rather diffuse, and it seems that the border-line between the two orthorhombic phases exists in this region. But the lattice constants show gradual changes even in this region.

(B) Lattice Change around the Transitions.

To examine the orystal structures of the intermediate phase and highest phase in the diagram shown in Fig. 12, we sludied the temperature dependence of crystal structure of KNbO₃, (K₋₁₀-Na₋₉₀)NbO₃, and NaNbO₃. The Unicam 19 cm. high temperature powder camera was used with Cu Ku radiation.

The orystal structures of KNbO3 at high temperatures were already studied by Wcod, and our re-examination shows complete agreement with the previous data, giving the tetragonal structure with n/s >1 between 220°C and

430°C, and the cubic structure above 430°C.

 $(K_{.10}-Na_{.90})NbO_3$ shows the same lattice type at room temperature as NaNbO_3, and it changes to tetragonal lattice with c/a > 1 at the phase transition of 240°C, and extra lines seem to disappear at the same tire. This tetragonal structure, therefore, is the same lattice type as in the intermediate phase of KNbO_3. The structure is cubic above 400° C.

The study of pure NaNbO₃ shows that this crystal is orthorhombic below 370°C, and the diffraction patterns taken above this temperature, e.g. 400°C, clearly show the lines of cubic perovskite. From this we can expect no more phase change at higher temperatures.

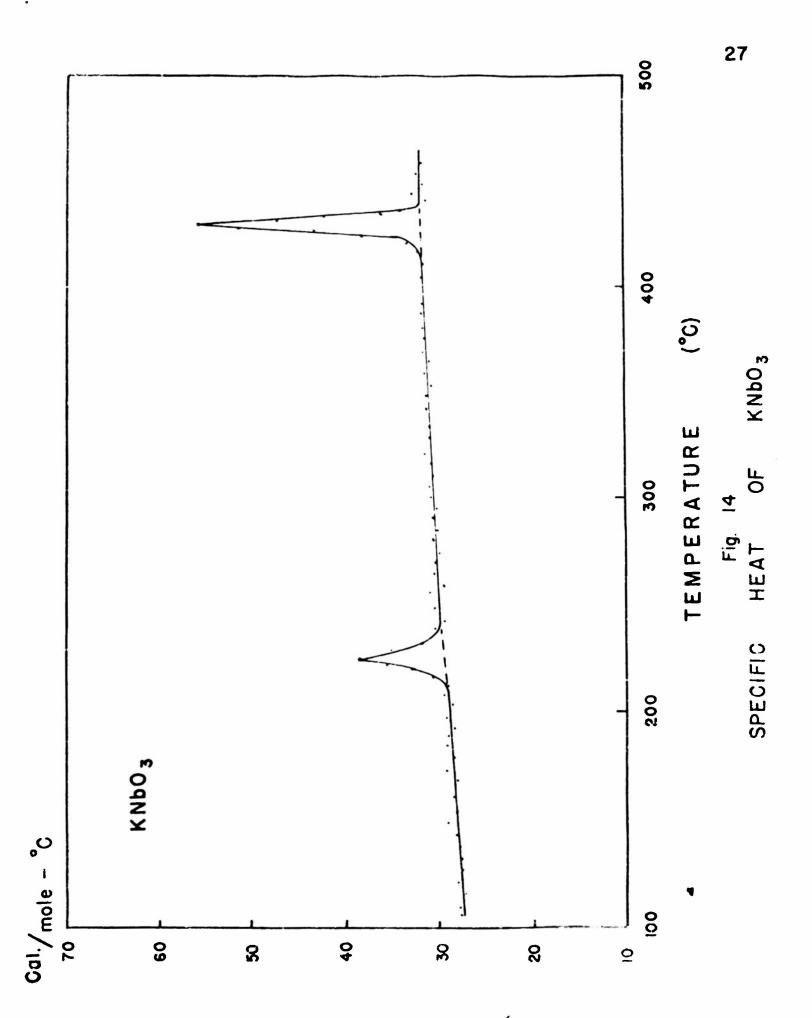
These results give the structural support for the phase diagram shown in Fig. 12.

IV. SPECIFIC HEAT MEASUREMENTS.

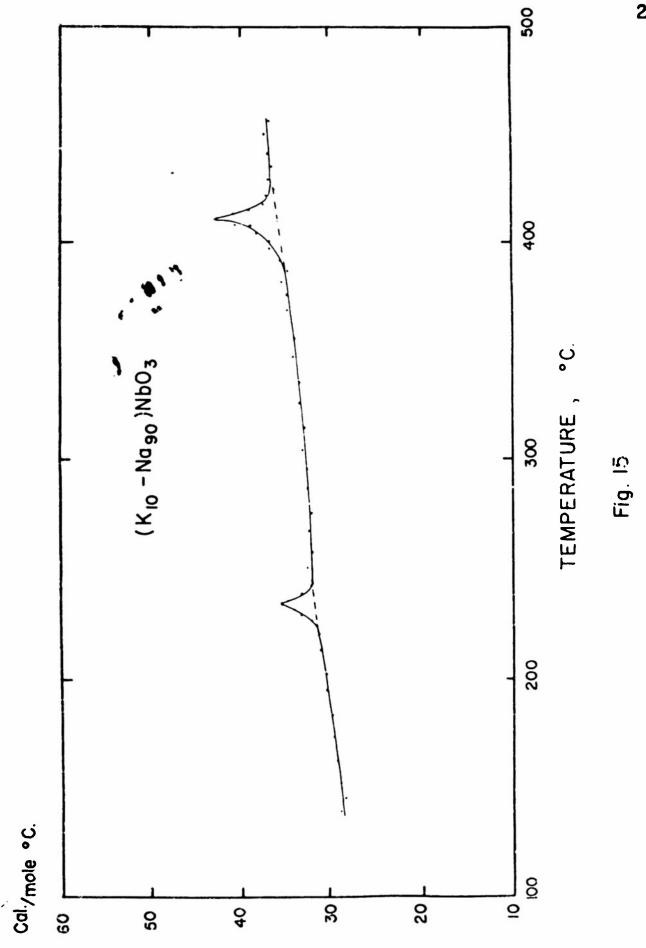
Specific heat vs temperature curves of KNbO3, (K.10-Na.90)NbO3 and NaNbO3 were measured by using an adiabatic calorimeter of Nagasaki-Takagi type (12), which is an improvement of Sykes' calorimeter. Detail of the construction of this calorimeter was described in a preceding report (13).

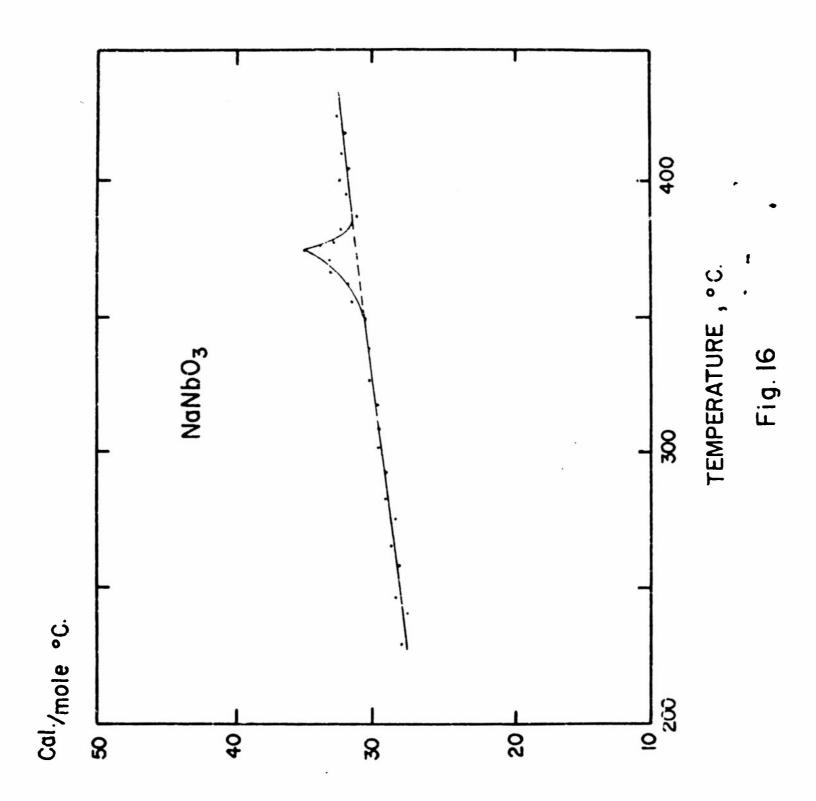
The specimen is a powdered ceramic prepared by the same method as the specimen for the dielectric and structural measurements. About 15 gms of material was placed in the Pt vessel, and heated at a rate of about 1°0/min. The heat content of the empty calorimeter was calibrated by using SiO₂ as a standard substance. The results are shown in Fig. 14-16.

From these curves we can easily see that NaNbO3 and (K.10-Na.90)NbO3 show rather small anomalies compared with the relatively large anomalies in KNbO3. By assuming a broken line shown in the figures as a normal specific









heat curve, we can obtain the integrated transition energies as follows:

	lower	phase change	upper	phase change
KNb03	85	cal/mole	190	cal/mole
(K _{.10} -Na _{.90})Nb03	20	cal/mole	60	cal/mole
NaNbO3			50	cal/mole

V. DISCUSSIONS.

Summarizing the above results, we can reach following conclusions:

(1) NaNbC₃ shows only one phase transition at 370°C, accompanied by a structural change from orthorhombic to cubic.

- (2) When a small amount of Na is replaced by K, the ferroelectric intermediate phase can be observed. This phase shows a tetragonal lattice with c/a>1, and it is the same phase as the intermediate phase of KNbO₃.
- (3) Concerning the ferroelectricity of pure NaNbO3, though the phase diagram suggests ferroelectricity in this crystal, but the absence of detectable hysteresis loops gives us strong doubt. This problem is still open to question, and must await the further study.

We must add here the following results, obtained very recently, after completion of the study of (K-Na)NbO3 system using ceramic specimen. Single crystals of NaNbO3 were prepared by the method used by Matthias and Remeika: namely, a mixture of NaNbO3, Nb2O5 and NaF was slowly cooled from 1500°C. Some of these single crystals show the dielectric anomalies at 370°C and 480°C in agreement with previous data and in contrast with our data on the ceramics. However, this phase change at 480°C may be explained by the small impurity contained in the crystal, because the phase diagram shown in Fig. 12 suggests that even small amount of impurity in NaNbO3 can easily result in another phase

change. Up to now, no hysteresis loops were observed in NaNbO3 single crystals. Further study of single crystals are now under way.

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